

Morphotropic phase boundary and electrical properties of $1 - x[\text{Bi}_{0.5}\text{Na}_{0.5}]\text{TiO}_3 - x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ lead-free piezoelectric ceramics

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Abstract

Lead-free solid solutions $(1 - x)\text{Bi}_{0.5}\text{Na}_{0.5}\text{TiO}_3$ (BNT)– $x\text{BaZr}_{0.25}\text{Ti}_{0.75}\text{O}_3$ (BZT) ($x=0, 0.01, 0.03, 0.05$, and 0.07) were prepared by the solid state reaction method. X-ray diffraction (XRD) and Rietveld refinement analyses of $1 - x(\text{BNT}) - x(\text{BZT})$ solid solution ceramic were employed to study the structure of these systems. A morphotropic phase boundary (MPB) between rhombohedral and cubic structures occurred at the composition $x=0.05$. Raman spectroscopy exhibited a splitting of the (TO_3) mode at $x=0.05$ and confirmed the presence of MPB region. Scanning electron microscopy (SEM) images showed a change in the grain shape with the increase of BZT into the BNT matrix lattice. The temperature dependent dielectric study showed a gradual increase in dielectric constant up to $x=0.05$ and then decrease with further increase in BZT content. Maximum coercive field, remanent polarization and high piezoelectric constant were observed at $x=0.05$. Both the structural and electrical properties show that the solid solution has an MPB around $x=0.05$.

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1. Introduction

Lead based piezoelectric ceramics are widely applied in electronic and microelectronic devices due to their excellent piezoelectric properties. However, the toxicity of lead oxide and its high vapor pressure during sintering processing cause serious environmental problem. So there is a huge demand of lead-free piezoelectric ceramic materials for various technological applications. Several works have been reported on the electrical properties of lead-free piezoelectric ceramics [1–4]. Among the various lead-free ceramics bismuth sodium titanate (BNT) is considered as a potential candidate for applications in piezoelectric devices.

This ceramic material exhibits strong ferroelectric properties with a relatively high Curie temperature. Moreover, the BNT-based materials possess an elevated anisotropic electromechanical coupling at a high frequency constant and lower dielectric constant [5] which justifies its applications in ultrasonic devices. Thus, the BNT-based ceramics have great prospects not only for environmental protection but also for different electronic applications.

The physical properties of BNT complex ceramic have been reported in 1961 by Smolenskii et al. [6]. Moreover it is also reported that this compound has a perovskite-type rhombohedral structure with formula $(\text{A}'\text{A}'')\text{BO}_3$ and space group $(R3c)$ in the temperature range of $25\text{--}200\text{ }^\circ\text{C}$ [7–12]. BNT exhibits a high coercivity ($E_c=73\text{ kV/cm}$), and considerable remanent polarization ($P_r=38\text{ }\mu\text{C/cm}^2$). This material is also mechanically tough, less toxic and also exhibits

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optical isotropism during the diffuse phase transition [13–17]. However, the major drawback of the BNT compound is its high conductivity. In order to obtain useful lead-free piezoelectric ceramic some modification in the BNT ceramic has been employed in the literature by diffusing with the other perovskites system to form solid solution [18–21]. Some recent works have been reported in the literature on the improvement of piezoelectric properties of BNT-based ceramics by making solid solutions [22–24]. This method is a trade-off to make use of the solid-solution technique to substitute the individuals and seek for the merits of the selected materials. BaTiO₃ and its doped species have been investigated to develop high-quality lead-free ceramics. It is observed that the substitution of Zr⁴⁺ ions by the Ti⁴⁺ ions in BaTiO₃ can significantly improve the overall properties of the material because of its better chemical stability [25]. The composition Ba[Zr_{0.25}Ti_{0.75}]O₃ (BZT) was chosen because it shows a diffuse phase transition behavior which is already reported by the author in a previous work [26].

Therefore in this paper, we report the structural and electrical properties of 1–*x*(BNT)–*x*(BZT) solid solution emphasizing the presence of morphotropic phase boundary (MPB).

2. Experimental details

2.1. Synthesis of 1–*x*(BNT)–*x*(BZT) ceramics

[Bi_{0.5}Na_{0.5}]TiO₃ (BNT) and Ba[Zr_{0.25}Ti_{0.75}]O₃ (BZT) ceramics were prepared by the conventional solid state reaction method separately. Reagent grade oxide or carbonate powder of bismuth oxide Bi₂O₃ (Merck, India; 99.9%), sodium carbonate Na₂CO₃ (Merck, India; 99.9%), barium carbonate BaCO₃ (Loba Chem., India, 99.9%), zirconium oxide ZrO₂ (Merck, India, 99.9%) and titanium oxide TiO₂ (Merck, India, 99.9%) were used as starting raw materials. Stoichiometric amounts of the starting reagents were ball-milled in ethanol media for 12 h. BNT samples were heat-treated at 850 °C for 2 h with intermediate grinding and mixing. The BZT samples were heat-treated at 1200 °C for 4 h with intermediate grinding and mixing. Appropriate amounts of single phase BNT and BZT powders were grinded for 4 h adding 5% polyvinyl alcohol as a binder. The granules were sieved and uniaxially cold pressed with a load of 6 t to obtain discs with a diameter of about 10 mm. The discs were decarbonized at 550 °C and then sintered at 1150 °C for 4 h in a covered alumina crucible with Bi₂O₃ powder in the crucible.

2.2. Characterizations

The crystalline structure of 1–*x*(BNT)–*x*(BZT) ceramic was analyzed by X-ray diffraction (XRD), (Xpert MPD, Philips, UK). The degree of structural order and phase solubility of the ceramic system was investigated by micro-Raman spectroscopy (ENWAVE OPTRONICS-EZRAMAN). The micro-Raman spectra were collected

using an Ar⁺ laser operated at excitation wavelength 633 nm. The microstructure of ceramics sintered at 1150 °C for 4 hrs was observed by scanning electron microscopy (SEM) (JEOL: JSM 6480LV, Japan). Silver paste was applied to both faces followed by heat treatment of the samples at 500 °C (20 min) for electrical measurements. Evolutions of the relative permittivity (ϵ_r) and dissipation factor ($\tan \delta$) with temperature were measured from room temperature (30 °C) to 475 °C, using an LCR meter (Hioki, Japan) operated in the frequency range from 40 Hz to 1 MHz. The dielectric data were taken every 5 °C, keeping a heating rate of 1 °C/min. The polarization versus electric field (P–E) loops of the specimens, were studied using a modified radiant automatic P–E loop tracer circuit by applying AC field. The sintered ceramic samples were polarized in silicone oil at 100 °C under 35 kV/cm for 20 min and piezoelectric constant (d_{33}) values of the samples were measured using a piezo- d_{33} meter (YE2730A d_{33} meter).

3. Results and discussions

3.1. X-ray diffraction and Rietveld refinement analyses

Fig. 1a and b illustrates the XRD patterns of 1–*x*(BNT)–*x*(BZT) ceramic with different compositions from 0 to 0.07 and reduced XRD patterns from 44° to 49° of these ceramics, respectively. The XRD patterns of all the 1–*x*(BNT)–*x*(BZT) ceramics can be indexed to a perovskite-type rhombohedral structure with the space group ($R\bar{3}c$). Moreover, it is observed that all the compositions are of single phase without the presence of any deleterious phases (Fig. 1(a)). This indicates that the BZT ceramic diffuses completely into the BNT lattice matrix to form a homogeneous 1–*x*(BNT)–*x*(BZT) ceramic solid solution. From the reduced XRD pattern as shown in Fig. 1(b), it is observed that there is no observable peak splitting for composition $x \leq 0.03$, indicating that these compositions have a pure rhombohedral symmetry. It is also observed that there is a shift in the peak towards the lower angle side indicating an increment in lattice parameter and cell volume with increase in BZT content due to the large radius of Ba²⁺ (1.61 Å) in relation to [Bi_{0.5}Na_{0.5}]²⁺ (~1.40 Å) [27]. With further increase in *x*, the (024) peak tends to split and the splitting becomes more and more obvious, suggesting that a new cubic phase appears. However in the XRD patterns of 1–*x*(BNT)–*x*(BZT) with $x=0.05$ it is observed that there is a considerable shift of angle (2θ) towards the higher side and consequently a reduction of lattice parameters.

The structural refinement of the 1–*x*(BNT)–*x*(BZT) ceramics with different *x* compositions from 0 to 0.07 was performed by MAUD software (version 2.33) [28–30] employing the Rietveld refinement method [31]. The results obtained from the Rietveld refinement show good agreement between the measured experimental XRD patterns and theoretical line profile (Fig. 2(a, b); Supplementary data Fig S1 (a–d)). It is also observed that the profiles of

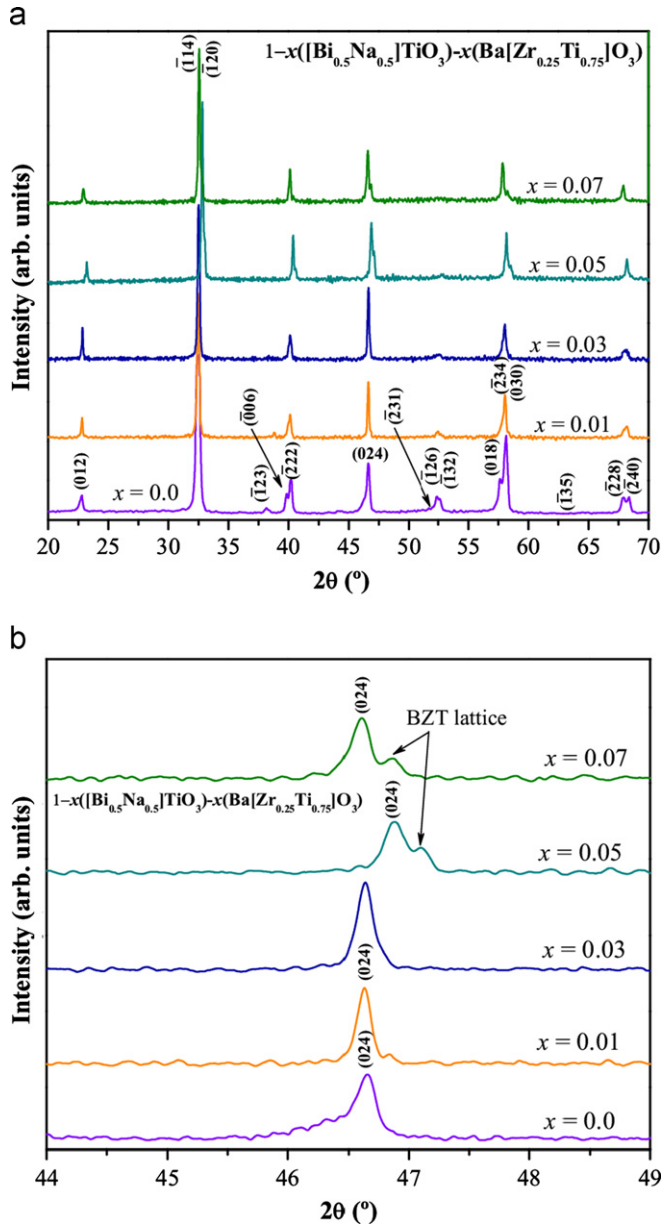


Fig. 1. (a) XRD patterns of $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x(\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3)$ ceramics and (b) XRD patterns in the range from 44° to 49° .

the XRD patterns experimentally observed and those theoretically calculated displays small difference as illustrated by a line $Y_{\text{Observed}} - Y_{\text{Calculated}}$. The lattice parameters and atomic positions obtained from the Rietveld refinement are listed in Table 1.

The fitting parameters (R_{wnb} , R_b , R_{exp} , R_w , and σ) suggest that the refinement results are reliable. In our work, the optimized parameters are scale factor, background with exponential shift, exponential thermal shift and polynomial coefficients, basic phase, microstructure, crystal structure, size-strain, structure solution model (genetic algorithm SDPD), shift lattice constants, profile half-width parameters (u , v , w), texture, lattice parameters (a , b , c), factor occupancy and atomic site occupancies (Wyckoff) [32,33].

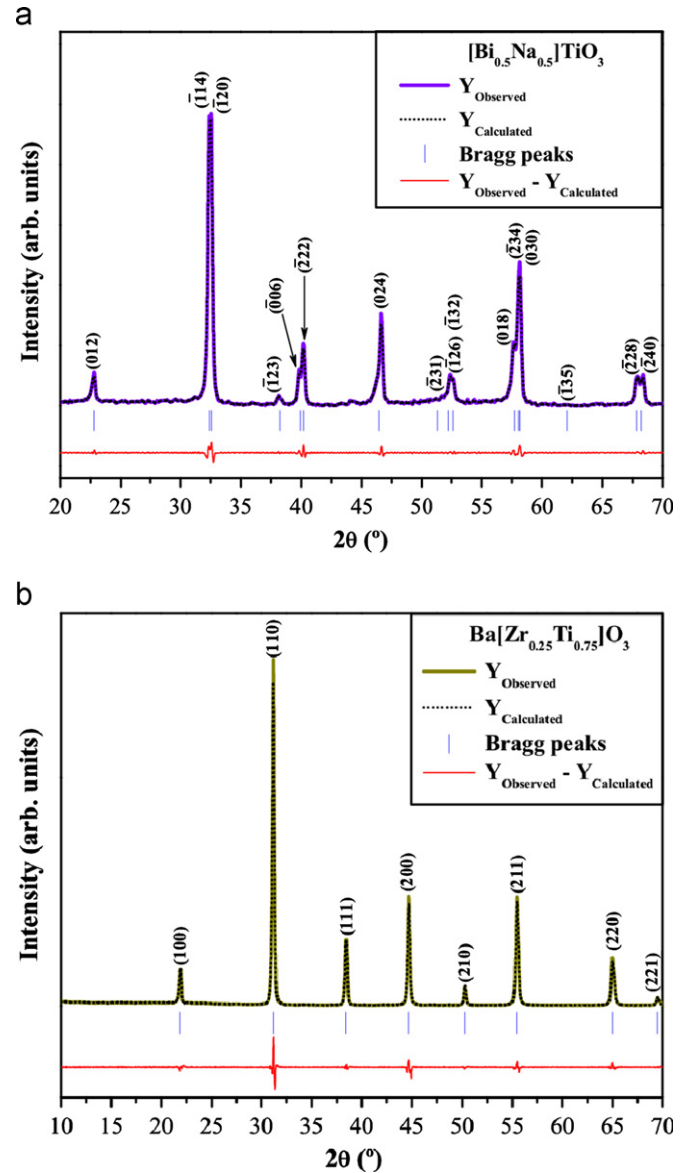


Fig. 2. Rietveld refinement plots of: (a) $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ and (b) $\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics.

In the Rietveld refinement, the measured diffraction patterns match the Crystallographic Information File (CIF) No. 154040 and 88533, for BNT and BZT structures, respectively [34,35]. In fact, the results arising from structural refinements are commonly acceptable under the following criteria: (a) $R_w < 10\%$ —medium complex phases (tetragonal, orthorhombic, rhombohedral and hexagonal); (b) $R_w < 15\%$ —high complex phases (monoclinic and triclinic) and (c) $R_w < 8\%$ —cubic structure (high symmetry and few diffraction peaks). Also, low σ values (< 2) indicate a good accuracy of the refinement results obtained [36]. Table 1 confirms a good fitting obtained with CIFs reported. These parameters were employed to model the unit cells of BNT and BZT ceramics by means of the visualization for electronic and structural analysis (VESTA) program (Version 3.1.0 for Windows) [37].

Table 1

Lattice parameters, unit cell volume, atomic coordinates and site occupation obtained by Rietveld refinement data for the $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ and $\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics.

Atoms	Wyckoff	Site	<i>x</i>	<i>y</i>	<i>z</i>
Bi	6a	3.	0	0	0.212651
Na	6a	3.	0	0	0.286785
Ti	6a	3.	0	0.5	0.041088
O	18b	1	0.0921515	0.177511	0.092341
<i>R</i> $\bar{3}c$ (161) – rhombohedral (<i>a</i> = <i>b</i> =5.4629(3); <i>c</i> =13.4835(4) Å; <i>c/a</i> =2.4682; <i>V</i> =348.19 Å ³) <i>R</i> _p =9.82%; <i>R</i> _{wp} =5.4%; <i>R</i> _{exp} =2.2% and <i>σ</i> =2.45					
Ba	1a	<i>m</i> –3 <i>m</i>	0	0	0
Zr	1b	<i>m</i> –3 <i>m</i>	0.5	0.5	0.5
Ti	1b	<i>m</i> –3 <i>m</i>	0.5	0.5	0.5
O	3c	<i>mm</i> 2.	0	0.5	0.5
<i>Pm</i> $\bar{3}m$ (221) – cubic (<i>a</i> = <i>b</i> = <i>c</i> =4.0563(4) Å; <i>c/a</i> =1; <i>V</i> =66.74 Å ³) <i>R</i> _p =3.97%; <i>R</i> _{wp} =6.45%; <i>R</i> _{exp} =2.6% and <i>σ</i> =2.48					

3.2. Representation for the $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ and $\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ lattice

Fig. 3a and b show the representations of the BNT ($1 \times 1 \times 1$) unit cells and BZT supercells ($1 \times 2 \times 2$) respectively. Fig. 3(a) illustrates the unit cell for BNT ceramic with trigonal or rhombohedral structure, space group ($R\bar{3}c$), point-group symmetry (C_{3v}^6) and two molecular formula per unit cell (*Z*=2) [38]. In this unit cell, bismuth (Bi) and sodium (Na) atoms are coordinated to six oxygens (O) atoms, which form the distorted octahedral $[\text{BiO}_6]$ and $[\text{NaO}_6]$ clusters (6-vertices, 6-faces and 12-edges) [39]. In addition the titanium (Ti) atoms are hexacoordinated to six O atoms, represented by the octahedral $[\text{TiO}_6]$ clusters (Fig. 3(a)). Fig. 3(b) illustrates the presence of four unit cells forming the supercell ($1 \times 2 \times 2$) for the cubic structure of the BZT ceramic. This lattice has a space group ($Pm\bar{3}m$), point-group symmetry (O_h^h) and one molecular formula per unit cell (*Z*=1). In this supercell of BZT, barium (Ba) atoms are coordinated to twelve oxygens atoms which form the polyhedrons with cuboctahedral configuration for the $[\text{BaO}_{12}]$ clusters. The cuboctahedron has twelve identical vertices which are formed by the meeting of two triangles and two squares, fourteen faces and twenty-four identical edges, and each vertex separates a triangle from a square [40], while the Ti and Zr atoms are bonded to six O atoms to form a polyhedron (octahedron) which are written as $[\text{TiO}_6]$ and $[\text{ZrO}_6]$ clusters [39].

3.3. Raman spectra analyses

Fig. 4 elucidates the Raman spectroscopy study of $1-x$ (BNT)– x (BZT) ceramic with *x*=0,0.01, 0.03, 0.05 and 0.07. The rhombohedral structure of BNT has 13 Raman-active modes, which can be represented as $\Gamma_{\text{Raman}}=7A_1+6E$. However, Fig. 4 displays only five Raman-active modes in the range from 100 to 1,000 cm^{-1} which is in agreement with the works reported by Rout et al. [41] and Eerd et al. [42].

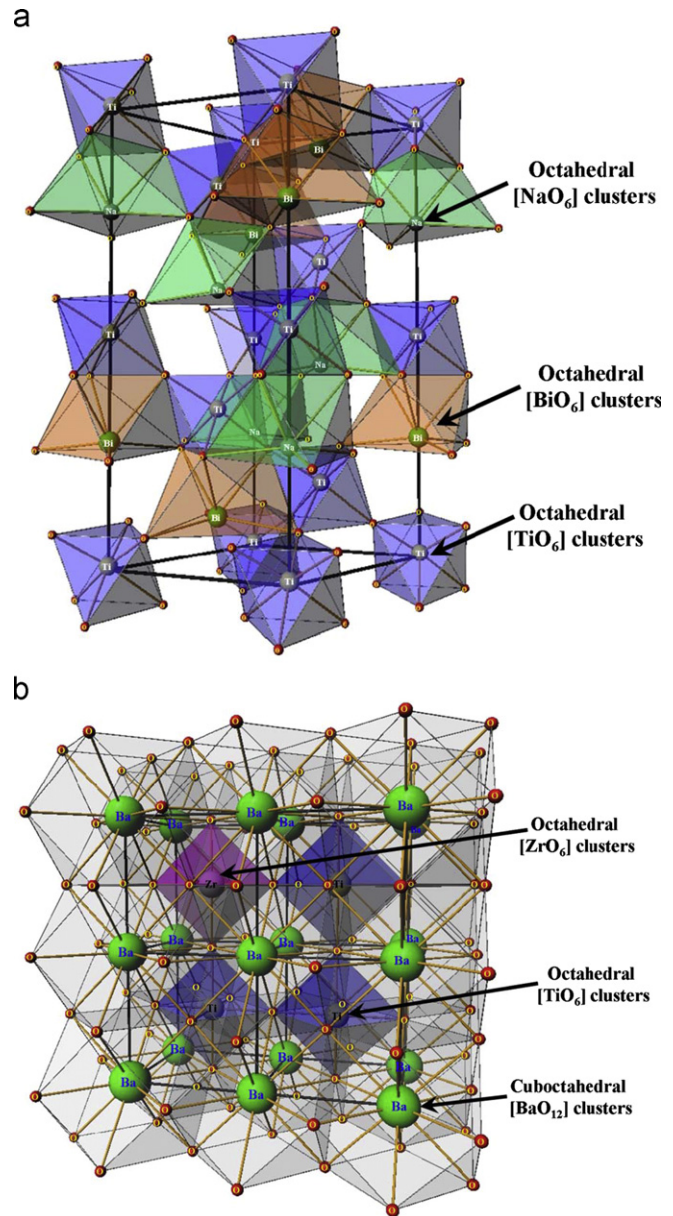


Fig. 3. Schematic representation of the unit cells for: (a) $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ ceramics and supercells for the: (b) $\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics.

Due to the disorder in the A-site related to distorted octahedral $[\text{BiO}_6]$ and $[\text{NaO}_6]$ clusters (Fig. 3(a)), this BNT ceramic with a rhombohedral structure has 13 Raman-active modes with the following representation: $\Gamma_{\text{Raman}}=4A_1+9E$ that have been analyzed and reported by Petzelt et al. [43]. The Raman peaks in Fig. 4 are relatively broad, which may be caused by distorted octahedral $[\text{BiO}_6]$ and $[\text{NaO}_6]$ clusters or disorder in the A-site of the rhombohedral structure. Also an overlap of Raman peaks is observed in all solid solutions. The first Raman-active $A_1(\text{TO}_1)$ mode at around (146 cm^{-1}) is related to network modifiers or distorted octahedral $[\text{BiO}_6]$ and $[\text{NaO}_6]$ clusters. The second Raman-active $E(\text{TO}_2)$ mode can be deconvoluted in three Raman peaks in 279 cm^{-1} regions. This mode is assigned to stretching arising from the bonds due to the presence of octahedral $[\text{TiO}_6]$ clusters at

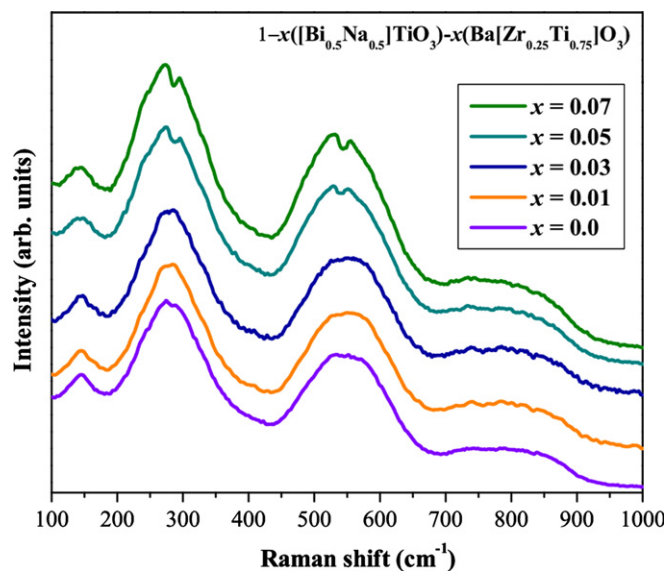


Fig. 4. Raman spectra of $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics.

short-range. The mode shows anomaly at $x=0.05$ and starts splitting into two bands that shift apart with further increase in the BZT content. The third Raman-active (LO_2) mode with low intensity is related to short-range electrostatic forces associated with the lattice ionicity [44]. According to Domenico et al. [45], the (TO_3) mode situated at around 542 cm^{-1} is ascribed to the ($\leftarrow\text{O}\leftarrow\text{Ti}\rightarrow\text{O}\rightarrow$) stretching symmetric vibrations of the octahedral [TiO_6] clusters. This mode is common in materials with perovskite-type structure. However the spectral signature of the band shows a change at $x=0.05$ and separates into two distinct bands at $x=0.07$. Finally, the (LO_3) mode found at 812 cm^{-1} is due to the sites within the rhombohedral lattice containing octahedral distorted [TiO_6] clusters [46]. These modes are classified into longitudinal (LO) and transverse (TO) components due to their electronic structures with a polar lattice character. However, Fig. 4 shows that all the Raman peaks are very broad. This behavior is possible due to disordered structure or distorted octahedral [TiO_6] clusters at short-range in both rhombohedral-BNT and cubic-BZT lattices.

3.4. Microstructural analyses

Fig. 5(a–e) shows SEM images of the $1-x(\text{BNT})-x(\text{BZT})$ ceramic ($x=0, 0.01, 0.03, 0.05$ and 0.07) sintered at 1150°C for 4 h. The pure BNT ceramics have a microstructure with rectangular grains, while the addition of BZT ceramic into the BNT matrix promotes a change to spherical grains (Fig. 5 (a–e)). The BNT disk appears to be poly-dispersed in both size and shape due to inhomogeneous grain growth. However, the addition of BZT ceramics results in the inhibition of grain growth, so the crystals of the BNT–BZT appear to be more uniform in both size and shape. Also the grain size is reduced with an increase in BZT content in compositions up to $x=0.03$ because Ba^{2+} is abundant in crystal boundary, which prevents the ion from migrating and

restrains growth between grains. The SEM image confirms that $1-x(\text{BNT})-x(\text{BZT})$ ceramics are densely sintered and all compositions have high density at around $5.67\text{--}5.83\text{ g/cm}^3$ which is more than 96% of the theoretical density. The Energy Dispersive X-ray Spectroscopy (EDS) of pure BNT and BNT–BZT compositions are shown in Fig. 6. The spectrum shows that all the elements are present with respect to their stoichiometry.

3.5. Dielectric properties analyses

Fig. 7 illustrates the temperature dependent dielectric behavior of $1-x(\text{BNT})-x(\text{BZT})$ ceramics with $x=0, 0.01, 0.03, 0.05$ and 0.07 at 100 kHz . It is seen from Fig. 6 that two dielectric peaks have been observed in each composition. The observed two dielectric peaks can be attributed to the factors caused by the phase transitions from ferroelectric to anti-ferroelectric, which is called depolarization temperature (T_d) and from anti-ferroelectric to paraelectric phase, at which the maximum value of dielectric constant corresponding temperature is the Curie temperature (T_m). The values of T_d and T_m are found to decrease with increase in the concentration of BZT, indicating that the conductivity of the materials is decreased compared with BNT. The MPB composition exhibits a lower depolarization temperature, which implies a reduction of the stability of ferroelectric domains. Compared with the compositions consisting of one single phase, the coexistence of a mixed rhombohedral–cubic phase could lead to more powerful stress in the MPB compositions, due to the incompatibility of their crystal lattices, resulting in a decrease of the thermal stability in the long-range ferroelectric domains [47]. The variation of dielectric constant (ϵ_r) with different x contents is given in Table 2. Moreover ϵ_r increases with an increase of BZT ceramic up to $x=0.05$ and decreases with a further increase in the x (BZT) content. This behavior can be assigned to substitution of Na, Bi, and Ti atoms (with atomic radius: 186 pm , 156 pm and 147 pm respectively) by Ba and Zr atoms (with atomic radius: 222 and 160 pm respectively) [47,48]. The addition of BZT in the BNT matrix makes the lattice structure incompact which is favorable for domain wall motion [49], hence the relative permittivity increases. Again Ba^{2+} doping also leads to a series of space charge centers and these space charge centers can disorder the distribution of electric potential, which can increase the potential barrier and the migration of the ions is restrained [50,51]. Meanwhile, further increase of BZT ($x=0.07$) ceramic into the BNT matrix leads to a decline in ϵ_r due to possible reaction of oxygen vacancies ($V_{\text{O}}^{\bullet\bullet}$). When the BZT content reaches its limit, further addition saturates the BNT lattice matrix and causes the clamping of wall domain [52]. This clamping will restrain the macro–micro domain switching in some degree; this is the reason that the relative permittivity declined at $x=0.07$.

The temperature dependent dielectric study shows a broad peak at phase transition (T_c) temperature indicating that the

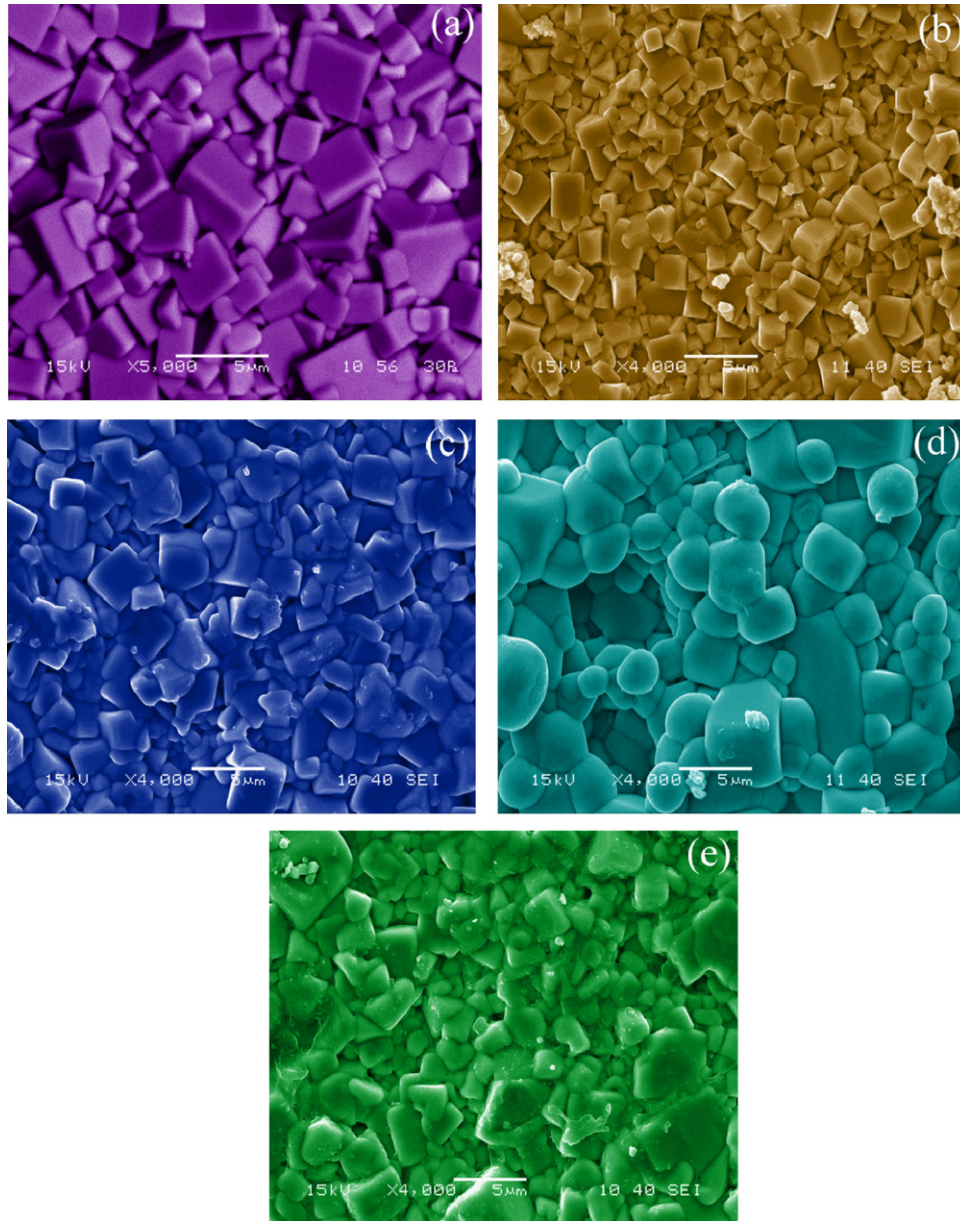


Fig. 5. SEM image for $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics with $x=0$ (a); $x=0.01$ (b); $x=0.03$ (c); $x=0.05$ (d); and $x=0.07$ (e).

phase transition is a diffuse type. The broadening or diffuseness of the peak may be due to the substitution disordering in the arrangement of cations at one or more crystallographic sites in the lattice structure leading to heterogeneous domains or may be due to the defect induced relaxation at high temperature [53–55]. The diffusivity parameter is been calculated by modified Curie–Weiss law, in Eq. (1) [56,57].

$$\frac{1}{\varepsilon} - \frac{1}{\varepsilon_m} = \frac{(T - T_m)^\gamma}{C_1} \dots (\text{at } T > T_m) \quad (1)$$

where γ and C_1 are constants for diffusion factor and Curie–Weiss constants, respectively. In general, the diffusion factor is between 1 and 2, representing the normal ferroelectric phase transition and diffuse phase transition. Plots of $\ln(1/\varepsilon' - 1/\varepsilon_m)$ as a function of $\ln(T - T_m)$ for all compositions are shown in

Fig. 8. The diffusion factor can be employed to describe the diffusion phase transition [58]. The diffusion factor compositional dependence is shown in Table 2. The diffusivity value increases with increase in BZT content indicating a relaxor behavior in the solid solution. The diffused phase transition behavior in BNT–BZT lead-free ceramics can be explained in terms of the coexistence of both polar rhombohedral structure and non-polar cubic structure with distorted octahedral $[\text{TiO}_6]$ clusters due to the cation disorder. In the BNT–BZT system Ba^{2+} and Zr^{4+} occupy A-site and B-site of ABO_3 perovskite structure respectively. In A-site Na, Bi and Ba have different valences and ionic radii, which results in the formation of the local electric fields owing to the local charge imbalance and the local elastic fields due to local structure distortions. Similar phenomenon also occurs at the B-site of

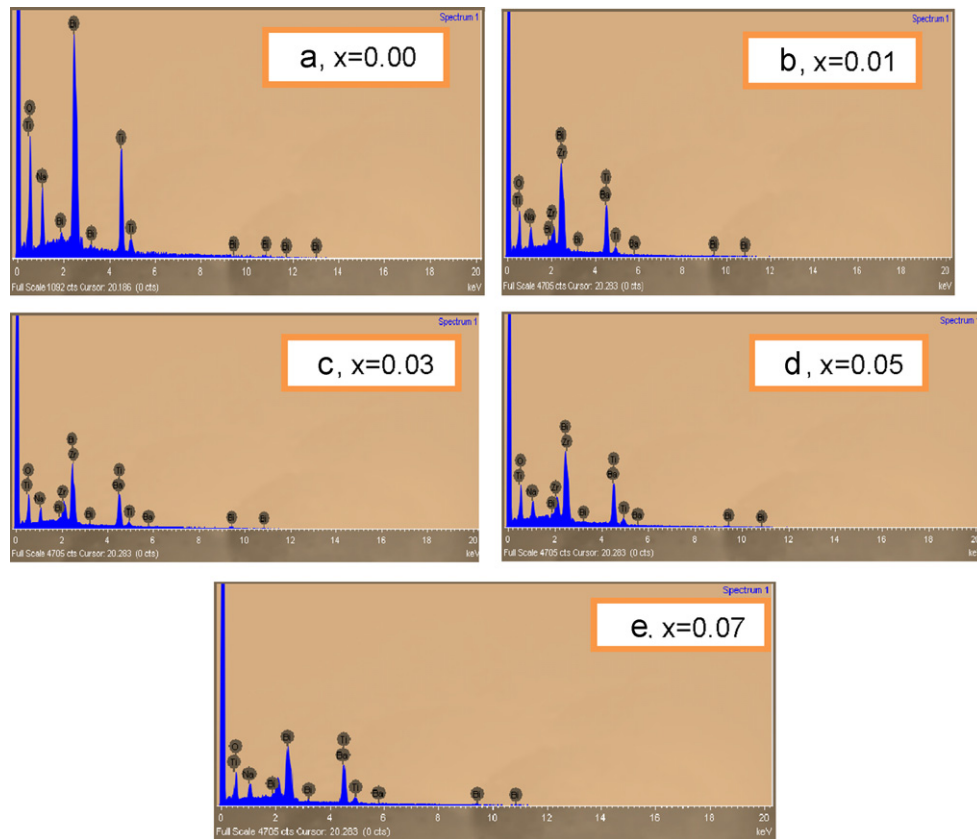


Fig. 6. EDS of $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics with $x=0$ (a); $x=0.01$ (b); $x=0.03$ (c); $x=0.05$ (d); and $x=0.07$ (e).

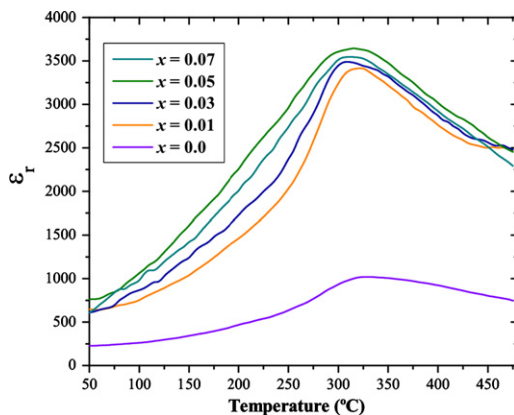


Fig. 7. Temperature dependence dielectric study of $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics at 100 kHz.

the ABO_3 perovskite structure. The presence of the random field including the local electric fields and elastic field hinders the long-range dipole alignment, i.e., giving rise to PNRs. These PNRs are isolated and frustrated in the system and are embedded in the disordered matrix, which results in the relaxor behavior. Consequently, the relaxor behavior of BNT–BZT ceramics is believed to result from the complex response of all the PNRs and matrices. Recently it was reported by Yao et al. [59] that the size of PNR decreases and the higher degree of self-organization increases as the

composition approaches the MPB. Such self-organization indicates that the system is able to relax its elastic energy by geometrically arranging the PNRs into improper ferroelastic domain bands. Stress accommodated finer PNRs would result in a polydomain structure, which is more susceptible to electric field E . So the diffusivity in the dielectric spectrum is maximum at the MPB region.

3.6. Ferroelectric properties analyses

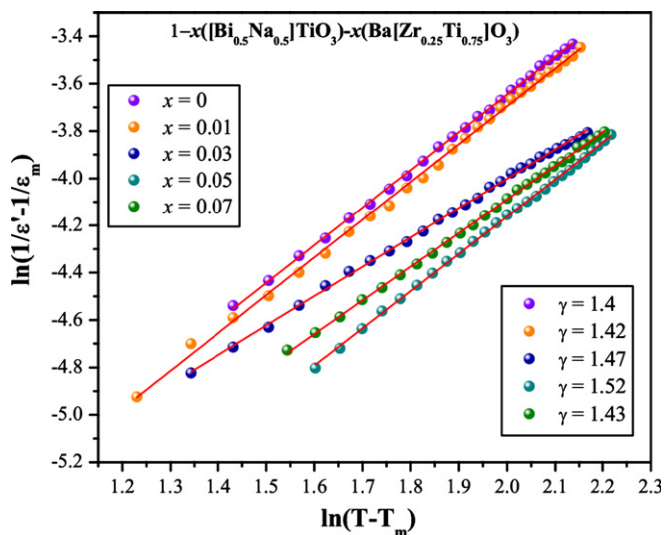
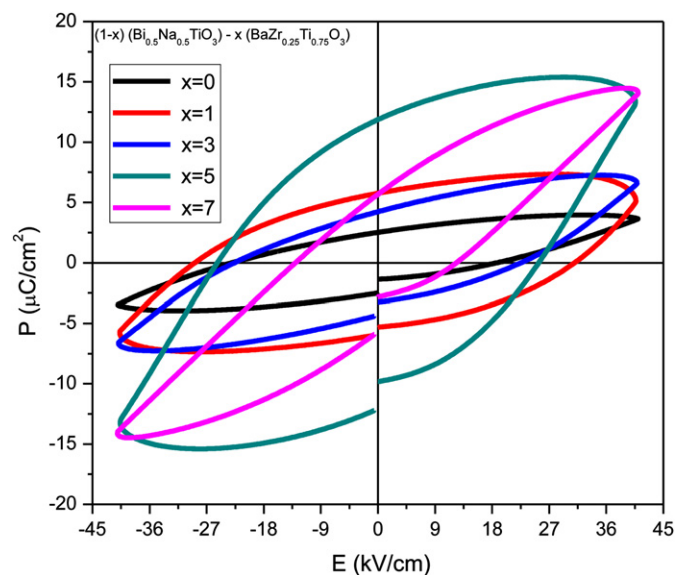
Fig. 9 shows P – E loops of $1-x(\text{BNT})-x(\text{BZT})$ ceramics with $x=0; 0.01; 0.03; 0.05$; and 0.07 with a maximum coercive field (E_c) of 42 kV/cm at room temperature.

In comparison with BNT ceramic, BNT–BZT ceramic shows an enhanced remanent polarization and coercive field, indicating a modification of ferroelectric properties. The variation in P_r and E_c is given in Table 1 which is related to structure parameters such as dc-a , α_R , and the cT/aT ratio. The value of E_c represents the difficulty of domain alignment, which is related to the degree of distortion of a unit cell. In general, a less distorted unit cell (i.e., close to a cube) usually accompanies a lower strain and a smaller E_c during domain alignment. The increase in E_c with increase in BZT content may be due to the increase of cT/aT ratio upto $x=0.05$. But a decrease in E_c occurs at $x=0.07$ due to the change of α_R toward 90° . The smallest E_c in the present system is found at $x=0.07$, a

Table 2

Dielectric, ferroelectric and piezoelectric coefficients of $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics.

$1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics	T_c (°C)	T_d	ϵ_m	γ	d_{33} (pC/N)	E_c (kV/cm)	P_r ($\mu\text{C}/\text{cm}^2$)
$x=0$	333	210	1020	1.4	41	20	2.5
$x=0.01$	327	190	3382	1.42	60	22.5	4.2
$x=0.03$	319	175	3427	1.47	87	25.2	5.8
$x=0.05$	310	155	3533	1.57	131	29.7	12
$x=0.07$	319	165	3416	1.42	111	12.6	5.7

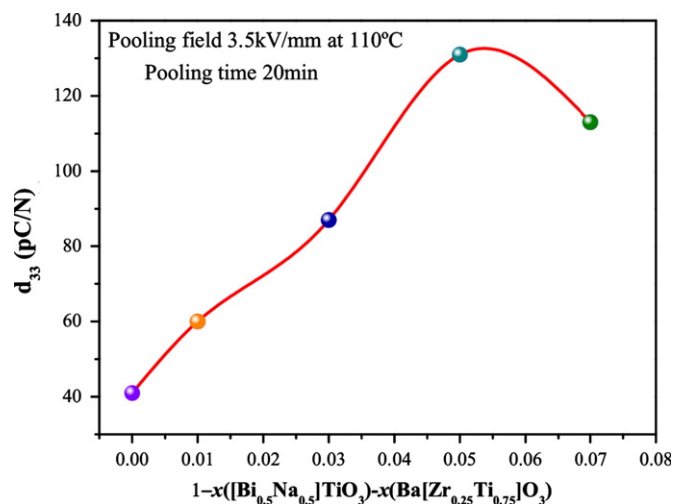
Fig. 8. $\ln(1/\epsilon - 1/\epsilon_m)$ vs $(T - T_m)$ of $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics at 100 kHz.Fig. 9. The P-E hysteresis loops of $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics.

cubic side of the MPB composition, but not at the MPB composition that also has been observed in other BNT-based ceramic systems [60,61]. Consequently, a significant decrease in E_c can be found in the BNT-based system as the composition is fully passing through the MPB region to the cubic phase, which also provides another method for determining the MPB composition. For the present work, an obvious decrease in E_c occurs from 5% to 7%, which reveals that $x=0.07$ is fully passing the MPB region. Therefore, $x=0.05$ is the MPB composition with coexisting rhombohedral and cubic phases, and that is in agreement with the crystal structure refinement result from the XRD pattern.

3.7. Piezoelectric properties analyses

Fig. 10 shows the compositional dependence of the piezoelectric coefficient d_{33} as a function of the $x\text{BZT}$ fraction.

The piezoelectric coefficient d_{33} increases with increase in BZT content and attains a maximum value of 131 pC/N for $x=0.05$ in the MPB region and then decreases to 111 pC/N for $x=0.07$. The increase in the piezoelectric constant d_{33} in the MPB composition may be attributed to an increase in the domain wall flexibility. Our results

Fig. 10. Composition vs. d_{33} for the $1-x(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{Ba}[\text{Zr}_{0.25}\text{Ti}_{0.75}]\text{O}_3$ ceramics.

indicate that the BNT-BZT system (similar to PZT) has MPB, and thus it possesses stronger piezoelectric properties which is in agreement with results reported by Lin et al. [62]. The ceramics crystal structure is considered

to be a coexistence of rhombohedral and cubic phases in the MPB composition. As the rhombohedral phase free energy is close to the cubic phase free energy, these two phases are easily exchanged by applying an electric field. In the close vicinity of MPB both the crystallographic phases are in thermal equilibrium with each other with vanishing polarization anisotropy [63]. Therefore, a flipping of polarization between two phases is possible on application of electric field. Enhanced piezoelectric coefficients are obtained in MPB regions and are attributed to an easy switch in the polarization vector between all allowed polarization orientations [64,65].

4. Conclusions

In summary, the BNT-based solid solution $1-x(\text{BNT})-x(\text{BZT})$ ceramics with $x=0; 0.01; 0.03; 0.05$ and 0.07 were prepared by the solid state reaction method. The MPB of rhombohedral and cubic phases was detected in the range at $x=0.05$ by the XRD patterns and Rietveld refinement data. Raman spectroscopy also indicated the presence of MPB in the solid solution. Enhanced electrical properties have been obtained at the MPB region with maximum dielectric constant, spontaneous polarization, coercive field and piezoelectric constant. In the MPB region, the polarization vector can easily switch (upon application of a small field) between all the allowed polarization orientations, and hence enhances the dielectric constant, and ferroelectric and piezoelectric coefficients. So the BNT–BZT system is expected to be a new and promising candidate for lead-free dielectric and piezoelectric material.

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