



## Full Length Article

Unveiling the shape-selective  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  nanomagnetismV. Jagadeesha Angadi<sup>a,b</sup>, K. Manjunatha<sup>c</sup>, Marisa C. Oliveira<sup>d</sup>, Elson Longo<sup>d</sup>, Sergio R. de Lázaro<sup>e</sup>, Renan A.P. Ribeiro<sup>f,\*</sup>, S.V. Bhat<sup>a,\*</sup><sup>a</sup> Department of Physics, Indian Institute of Science, Bangalore 560012, India<sup>b</sup> Department of Physics, P.C. Jabin Science College, Hubballi 580031, India<sup>c</sup> Department of Physics, School of Engineering, Presidency University, Bangalore 560064, India<sup>d</sup> Center for the Development of Functional Materials (CDMF), Federal University of São Carlos, São Carlos, SP, Brazil<sup>e</sup> Department of Chemistry, State University of Ponta Grossa, Ponta Grossa, PR, Brazil<sup>f</sup> Department of Chemistry, Minas Gerais State University, Divinópolis, MG, Brazil

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## ABSTRACT

In this study  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  ( $y = 0, 0.01, 0.02, \text{ and } 0.03$ ) nanoparticles (NPs) have been synthesized following the solution combustion method and characterized by combining experimental techniques with high-throughput Density Functional Theory calculations. The structural analysis confirmed the crystalline nature with spinel cubic structure exhibiting an average particle size between 7 and 10 nm. The morphological analysis confirmed the exposure of the (220), (311), (400), and (422) planes in agreement with theoretical results based on Wulff Construction. Magnetic analysis indicated the existence of paramagnetic to ferrimagnetic phase transition at the critical temperature ( $T_c$ ) and a conical spiral spin phase was found at the spiral transition temperature ( $T_s$ ). In both the cases, the transition temperature was seen to decrease with increase in the Sc content in agreement with the exchange-coupling constants calculated by DFT, where a singular magneto-structural behavior was observed. Theoretical results for shape-oriented magnetic properties indicate the anisotropic spin density distribution and surface exposure, providing a general picture of shape-selective control of nanomagnetism.

## 1. Introduction

Spinel chromites with the general formula  $\text{ACr}_2\text{O}_4$  have received good scientific attention due to their promising applications in diverse areas such as in electrochemical sensors, biomedical materials, catalysis, spintronics, magnetic resonance imaging, and high-temperature ceramics [1–4]. They are also investigated for their interesting properties [5–7]. In these compounds, the magnetic and ferroelectric properties coexist and the magnetic properties can be controlled by electric field and vice versa thus making them technologically significant for switching devices, random access memories, and magnetoelectric memories [8].

Cobalt chromite ( $\text{CoCr}_2\text{O}_4$ ) is a ferrimagnetic material having a spinel structure with space group  $Fd-3m$  [9]. It is a normal spinel where  $\text{Co}^{2+}$  ions occupy the A sites and  $\text{Cr}^{3+}$  ions occupy the B sites of the spinel structure. [10]. The  $\text{CoCr}_2\text{O}_4$  nanoparticles (NPs) exhibit long-range ferrimagnetic order below the critical temperature ( $T_c$ ) and non-collinear conical spiral spin order at a spiral transition temperature ( $T_s$ ) [11,12]. At low temperatures, cobalt chromite NPs show interesting

behaviour in their magnetic properties. Zakutna et al. [13] reported a size-based glassy-like state in  $\text{CoCr}_2\text{O}_4$  NPs. Rath et al. [14] observed a spin-glass structure in  $\text{NiCr}_2\text{O}_4$  NPs resulting from interactions among surface and ordered core spins. However, Mohanty et al. [12,15] observed that the position of the ac-susceptibility peak of  $\text{CoCr}_2\text{O}_4$  NPs did not change with frequency, ruling out the possibility of a spin-glass-like structure in the sample. Rath et al. [16,17] studied the transitions in  $\text{CoCr}_2\text{O}_4$  NPs and found an intermediate superparamagnetic phase between  $T_c$  and the blocking temperature which was somewhat higher than  $T_s$ . They attributed this behavior to disordered spin configuration at the surfaces and the distribution of NP sizes. Ptak et al. [18] in their magnetic and IR studies of  $\text{CoCr}_2\text{O}_4$  NPs found the evidence for the development of an incommensurate phase below  $T_s$  and also for spin phonon coupling. Tian et al. [19] found a decrease in both  $T_c$  and  $T_s$  in  $\text{CoCr}_2\text{O}_4$  NPs which they attribute to the spin disorder produced at the surface of the NPs. Chen et al. [20] observed that in  $\text{CoCr}_2\text{O}_4$ , commensurate and incommensurate spiral orders coexist. With application of high pressure they found a rise in  $T_s$  and lock-in transition temperature ( $T_l$ ) caused by lattice contraction leading to more

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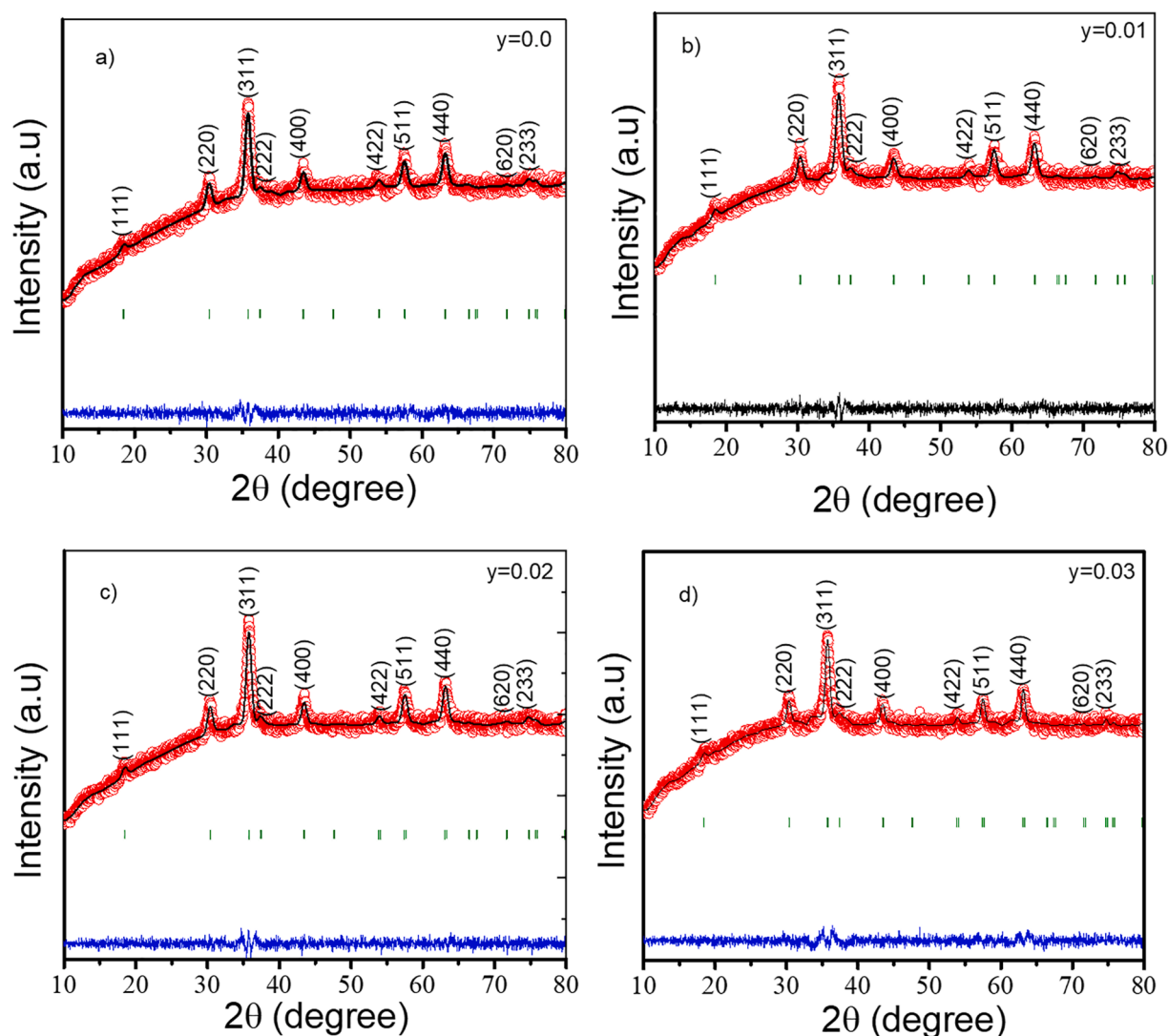


Fig. 1. Rietveld refined XRD patterns of the as-synthesized  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  for a)  $y = 0.0$ , b)  $0.01$ , c)  $y = 0.02$  and d)  $y = 0.03$ .

Table 1

Experimental values for lattice parameter, crystallite size (diameter) and Rietveld refinement parameters ( $R_p$ ,  $R_{wp}$ ,  $R_{exp}$  and  $\chi^2$ ) of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  ( $y = 0, 0.01, 0.02$  and  $0.03$ ) samples.

| Sc <sup>3+</sup> content | Lattice parameter (Å) | Crystallite size (nm) | $R_p$ | $R_{wp}$ | $R_{exp}$ | $\chi^2$ |
|--------------------------|-----------------------|-----------------------|-------|----------|-----------|----------|
| $y = 0$                  | 8.3229                | 10                    | 1.52  | 1.90     | 1.78      | 1.15     |
| $y = 0.01$               | 8.3259                | 9.5                   | 1.41  | 1.78     | 1.66      | 1.14     |
| $y = 0.02$               | 8.3276                | 10                    | 1.42  | 1.79     | 1.71      | 1.10     |
| $y = 0.03$               | 8.3294                | 9.6                   | 1.48  | 1.88     | 1.72      | 1.20     |

significant magnetic frustration.

Control of  $\text{CoCr}_2\text{O}_4$  magnetic properties through site-selective doping i.e., doping in either tetrahedral or octahedral sites from the point of view of technological applications is currently an active area of research [5,9,21–31]. We have recently studied the effects of the Bi- and Sc-doping in  $\text{CoCr}_2\text{O}_4$  NPs, providing compelling evidence that tetrahedral site doping modifies exchange coupling strength between Co-Co, Co-Cr, and Cr-Cr resulting in singular magneto-structural behavior [32,33]. Motivated by the literature referred to above, herein, the structural, microstructural, and magnetic behaviors of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  ( $y = 0, 0.01, 0.02$ , and  $0.03$ ) NPs are investigated through a combined experimental-theoretical study.

## 2. Experimental

### 2.1. Sample preparation

Stoichiometric amounts of metal nitrates like cobaltous nitrate, scandium nitrate, and chromium nitrate, as well as fuels like glucose and urea (details in [Supporting Information](#)), were dissolved in distilled water in a glass beaker and stirred for one hour with a magnetic stirrer to obtain a homogeneous solution. The solution was heated at  $450^\circ\text{C}$  in a preheated box-type muffle furnace. The fluid initially boiled, frothed, and then ignited. Within 20 min, the combustion process was completed. The resulting material was crushed into a fine powder with an agate mortar and pestle.

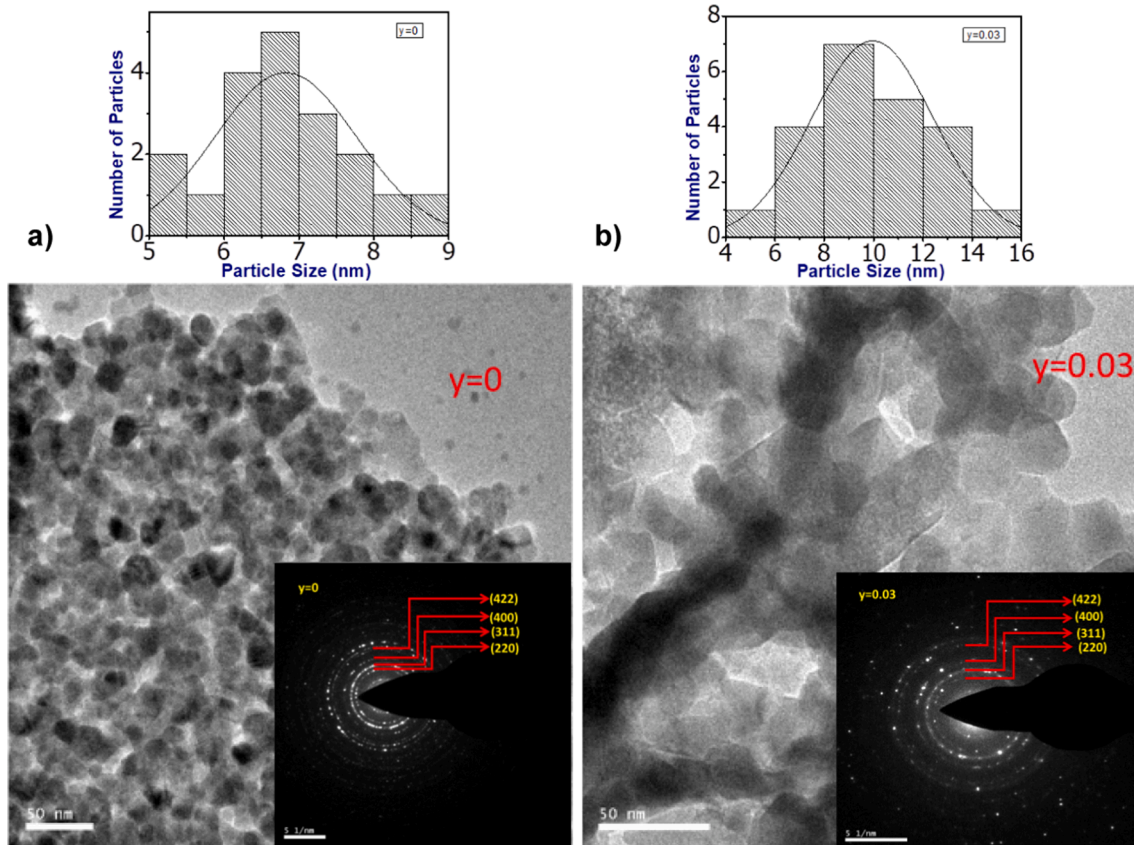


Fig. 2. TEM images, Particle size distribution histograms and SAED patterns of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  NPs with a)  $y = 0.0$  and b)  $y = 0.03$ .

## 2.2. Sample characterization

X-ray diffraction (XRD) patterns of the samples were recorded using a 'PANalytical X-ray diffractometer' with Cu-K radiation ( $\lambda = 1.54056 \text{ \AA}$ ) in the  $2\theta$  range of  $10\text{--}80^\circ$  with a step size of  $0.02^\circ$ . Rietveld refinement of the patterns was carried out using the FULLPROF software to obtain the crystal structure parameters. Scherrer formula was used to determine the particle size. As regard the analysis of Sc-content, it is important to mention that only stoichiometric estimative were considered (details in [Supporting Information](#)), once elemental-based analysis were not available due to the COVID-19 pandemic. Transmission electron microscopy (TEM) images and selective area electron diffraction (SAED) patterns were recorded on a Philips (JEM-2100 TEM) instrument. The samples were examined under this TEM after dispersing the sample in ethyl alcohol and placing it on a copper grid. TEM generates the high-resolution image of lattice structure of the crystalline material which gives the direct characterization of the sample's atomic structure. Further, the particle size distribution of the samples was estimated by using ImageJ software. The magnetization investigations were performed by using a SQUID magnetometer at 500 Oe field in the temperature range from 2 to 400 K. The susceptibility ( $\chi$ ) was calculated by using  $\chi = \frac{M}{H}$ , where M is the measured magnetization and H is the applied field. The field dependent magnetization (M–H loops) was studied by using the SQUID magnetometer at three different temperatures (10, 95, and 300 K) in the field range  $\pm 20,000$  Oe.

## 2.3. Density functional theory calculations

CRYSTAL17 [34] was used to perform density functional theory calculations utilizing the non-empirical PBE0 hybrid functional [35]. The electronic structure of oxide materials is well described by hybrid exchange–correlation functionals (B3PW, PBE0, and B3LYP) [36,37],

with PBE0 being the most trustworthy choice for multiferroic materials [38].

The supercell expansion (112-atoms) was used to create theoretical models for  $\text{CoCr}_2\text{O}_4$  and  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  models. In addition, the isoelectronic substitution of  $\text{Cr}^{3+}$  by  $\text{Sc}^{3+}$  was studied for Sc-doped models.

Three Ferrimagnetic (FiM) collinear models were used to determine the exchange-coupling constant compared to Ferromagnetic orientation (FEM). Herein, the primitive  $\text{CoCr}_2\text{O}_4$  cell comprising 14-atoms can be used to describe the magnetic orientation once two Co and four Cr atoms are surrounded by eight O atoms, resulting in a FEM model ( $\text{Co}_{\uparrow}\text{Cr}_{\uparrow\uparrow\uparrow}$ ). The FiM-1, FiM-2, and FiM-3 were described as ( $\text{Co}_{\downarrow}\text{Cr}_{\uparrow\uparrow\uparrow}$ ), ( $\text{Co}_{\uparrow}\text{Cr}_{\uparrow\uparrow\uparrow}$ ), and ( $\text{Co}_{\uparrow}\text{Cr}_{\downarrow\downarrow\downarrow}$ ), respectively. [33] The Ising model estimated the exchange-coupling constant (J) based number of atom neighbors  $i$ – $j$  (Z) and the electronic spin of different species (S):

$$\hat{H}_{\text{ising}} = \sum J_{ij} \hat{S}_i \hat{S}_j \quad (1)$$

$$\Delta E_{\text{FiM-FEM}} = -2 \sum Z_{ij} S_i S_j J_{ij} \quad (2)$$

Moreover, the (100), (110), (111), and (311) surfaces for  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  were modeled combining a thermodynamic method with spin density analysis, as reported in earlier studies [32,39–49].

The lattice parameters and atomic locations were relaxed for all models. The reciprocal space based on the Monkhorst-Pack approach for bulk (surface) models was represented using  $8 \times 8 \times 8$  ( $4 \times 4 \times 4$ ) shrinkage factors, which was a suitable mesh to explain the electrical and energetic characteristics [50]. Co, Cr, and O atoms were characterized using an all-electron basis set [51–53], while Sc centers were described using an effective-core pseudopotential [54].

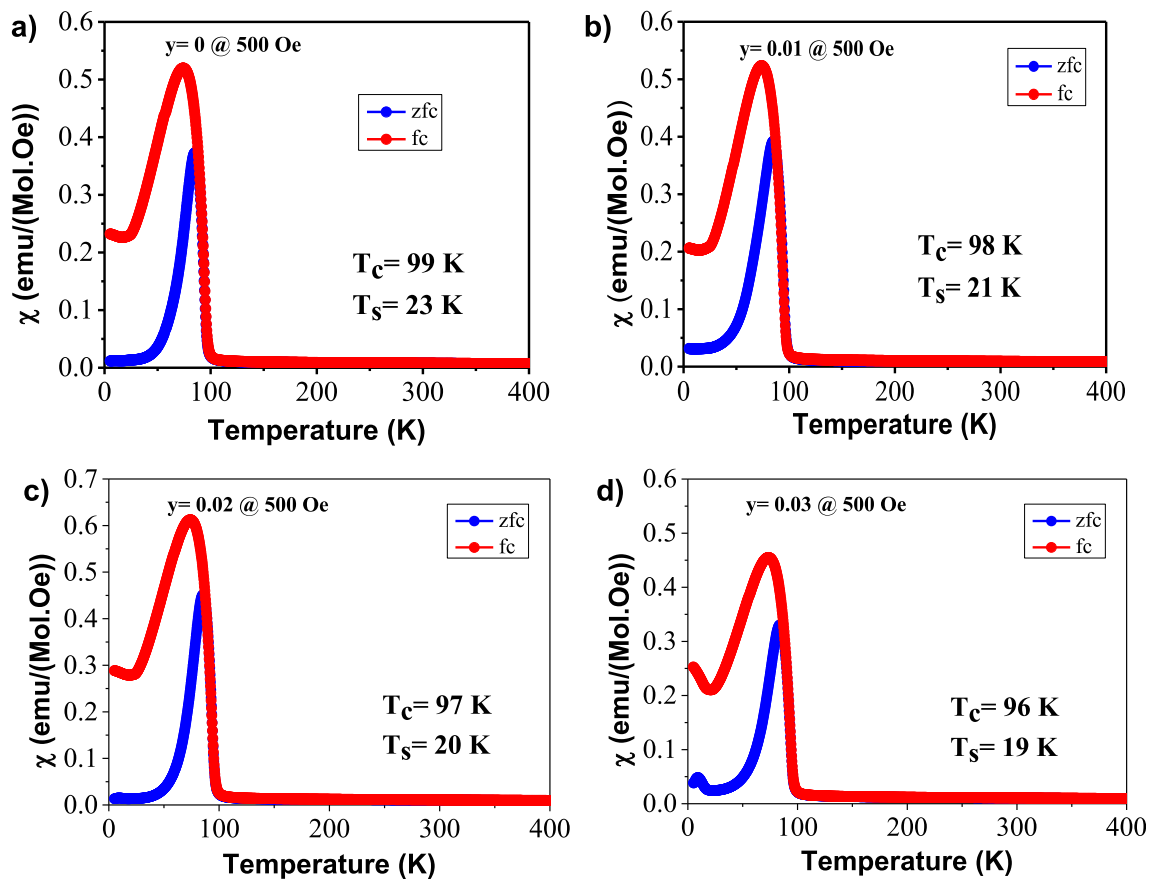


Fig. 3. Temperature dependent susceptibility  $\chi(T)$  of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  for a)  $y = 0$ , b)  $y = 0.01$ , c)  $y = 0.02$  and d)  $y = 0.03$  NPs.

### 3. Results and discussion

#### 3.1. Structural analysis

The XRD patterns for the as-synthesized  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  ( $y = 0, 0.01, 0.02$  and  $0.03$ ) samples are shown in Fig. 1. The patterns are characteristic of a single phase with a spinel cubic structure and the patterns match well with JCPDS file no. 780711 [33]. The figure also shows the results of Rietveld refinement carried out using the FULLPROF software. During the refinement the crystal structure and profile parameters such as lattice constants, atomic coordinates, occupancy of the ions, isotropic temperature factors, background corrections, peak shape parameters, symmetry and asymmetric parameters were refined so that the difference between the observed experimental XRD data and the calculated diffraction patterns was minimized by using least squares procedure. The results of the refinement are presented in Table 1 which lists the structural characteristics, phase composition and Rietveld refinement parameters ( $R_p$ ,  $R_{wp}$ ,  $R_{exp}$  and  $\chi^2$ ). The average crystallite size (diameter  $D$ ) was estimated by using Scherrer method.  $D$  was calculated from the widths of diffraction peaks using the Scherrer equation (3)

$$D = \frac{0.9\lambda}{\beta \cos\theta} \text{ nm} \quad (3)$$

where  $\lambda$  is the X-ray wavelength (in our experiment  $\lambda = 1.54056 \text{ \AA}$ ),  $\beta$  is the diffraction peak full width at half maximum (in radians),  $\theta$  is the angle of diffraction, and 0.9 is the Scherrer constant. Using this method, we calculated the mean size of crystallites from the width of the [311] peak at  $2\theta = 35.71$ . Table 1 also summarizes the crystallite size values along with the lattice characteristics. It is seen that the lattice parameter increases as  $\text{Sc}^{3+}$  concentration increases. This is as expected because  $\text{Sc}^{3+}$  ions have a higher ionic radius ( $0.745 \text{ \AA}$ ) than that of the  $\text{Cr}^{3+}$  ions

( $0.52 \text{ \AA}$ ).

#### 3.2. Morphological analysis

TEM images, particle size distribution histograms, and Selected Area Electron Diffraction (SAED) patterns of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  samples with  $y = 0.0$  and  $0.03$  are shown in Fig. 2, indicating a non-uniform shape for pure samples that becomes more faceted with the Sc-doping. The average particle size is 7 nm and 10 nm for  $y = 0$  and  $y = 0.03$ , respectively. These values are well-matched with the average crystallite sizes calculated from the X-ray diffraction, showing the polycrystalline nature of the particles. The spotty ring patterns identified with the (220), (311), (400), and (422) planes from SAED confirm the crystallinity of the NPs.

#### 3.3. Magnetic analysis

Fig. 3 shows the temperature-dependent susceptibility  $\chi(T)$  of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  ( $y = 0, 0.01, 0.02$ , and  $0.03$ ) obtained from magnetization measurements carried out in zero-field cooled and field cooled conditions at an applied magnetic field of 500 Oe. In all cases, the samples were warmed to 400 K to ensure that the sample regained the paramagnetic phase.

All the samples showed a rapid increase of FC and ZFC susceptibilities at a specific temperature (i.e., the critical temperature,  $T_c$ ) on decreasing the temperature from 400 K, indicating the paramagnetic to a long-range ferrimagnetic phase transition. The  $T_c$  values were obtained as 99 K, 98 K, 97 K, and 96 K for  $y = 0, 0.01, 0.02$ , and  $0.03$ , respectively, which are close to the data obtained by Tomiyasu et al. [55] for  $\text{CoCr}_2\text{O}_4$  single crystal and by Pronin et al. [56] for polycrystalline  $\text{CoCr}_2\text{O}_4$ .

Below the critical temperature, as the temperature decreases, the FC

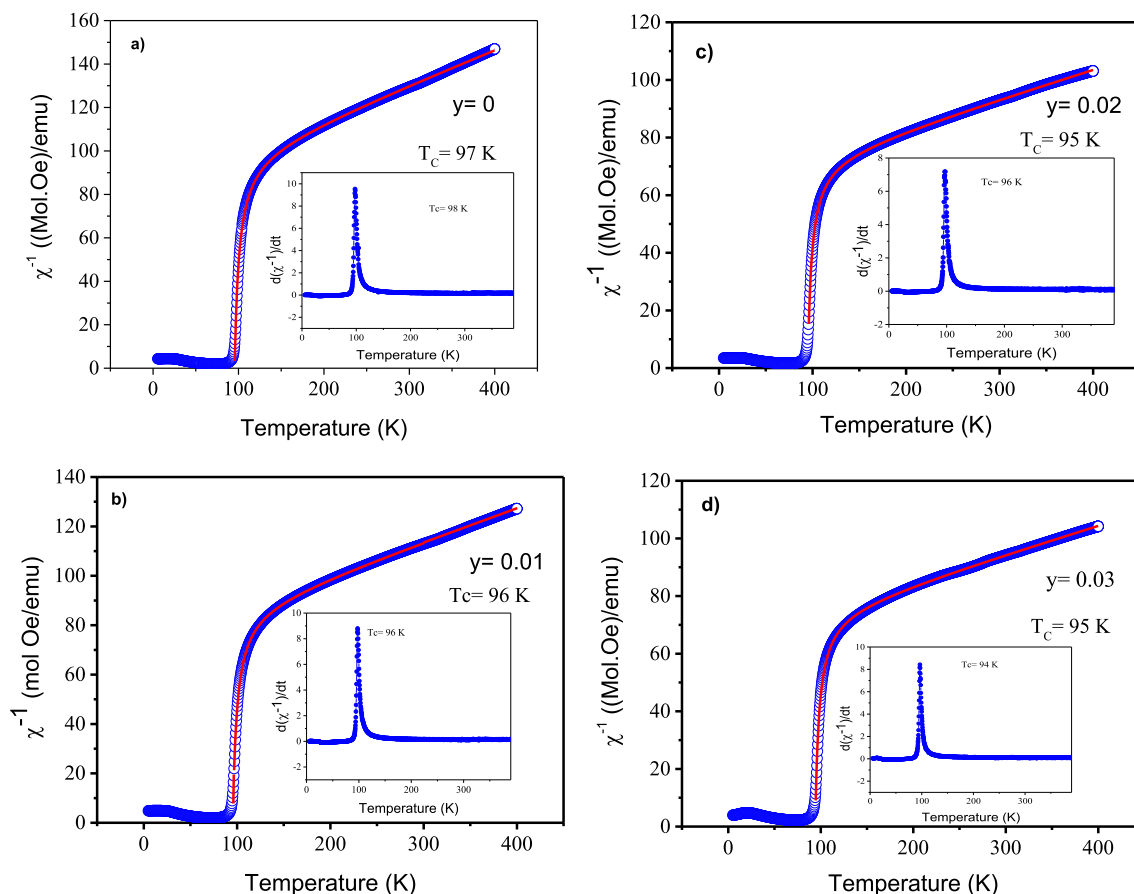


Fig. 4. Temperature dependence of reciprocal susceptibility of FC magnetization and its derivative (inset) for  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  a)  $y = 0$ , b)  $y = 0.01$ , c)  $y = 0.02$  and d)  $y = 0.03$  NPs.

curve shows an anomaly associated with the conical spin-spiral order phase, i.e., spiral transition temperature ( $T_s$ ). The  $T_s$  values were found to be 23 K, 21 K, 20 K and 19 K for  $y = 0, 0.01, 0.02$  and  $0.03$ , respectively.

To understand the critical behavior of the samples, we adopted equation (4) containing a Curie-Weiss (ferrimagnetic) term and a Curie (paramagnetic) term to fit the temperature-dependent reciprocal of susceptibility  $\chi^{-1}(T)$  as shown in Fig. 4:

$$\chi^{-1}(T) = \left( \frac{T}{C} + \frac{1}{\xi} \right) - \left( \frac{b}{T - \Theta'} \right) \quad (4)$$

where  $\chi^{-1}$  is the reciprocal susceptibility,  $C$  is the Curie constant,  $T$  is the temperature,  $\xi$ ,  $\Theta'$  and  $b$  are constants [9]. The paramagnetic term's presence is related to the no saturation behavior exhibited by chromites [57]. The high-temperature experimental data (paramagnetic) is well fitted by equation (4) with a deviation happening close to the Curie temperature. The obtained theoretical values for critical temperatures are  $T_c \sim 97, 96, 95$ , and  $95$  K for  $y = 0, 0.01, 0.02$ , and  $0.03$ , respectively, showing an excellent agreement with the experimental results. In spinels, the critical temperature ( $T_c$ ) is controlled by the exchange interaction between ions at the tetrahedral and octahedral sites. Therefore, the observed decrease in the critical temperature with the increase of  $\text{Sc}^{3+}$  concentration suggests that the exchange interaction between the tetrahedral and octahedral sites weakens because of substitution of  $\text{Cr}^{3+}$  ions by  $\text{Sc}^{3+}$  ions in the octahedral site. Our results on Sc-doped  $\text{CoCr}_2\text{O}_4$  nanoparticles show that both  $T_c$  and  $T_s$  decrease as the Sc concentration increases. One possible reason for this could be the random distribution of  $\text{Sc}^{3+}$  ions at the tetrahedral and octahedral sites. The structural analysis, on the other hand, confirmed that the lattice

parameter increases with increasing Sc concentration. As a result, the weakening of the magnetic transition at the spiral transition temperature in Sc doped  $\text{CoCr}_2\text{O}_4$  nanoparticles is a result of an intrinsic change in noncollinear to collinear spin structure of B sites in  $\text{CoCr}_2\text{O}_4$ , and following [58] it is directly related to the system's lattice disorder. The lattice disorder in Sc doped  $\text{CoCr}_2\text{O}_4$  nanoparticles leads to a decrease in B site direct interactions which results in a change in B site spin structure from noncollinear to collinear.

Further, the magnetization as a function of applied magnetic field at different temperatures was investigated, as shown in Fig. 5. For all samples, the linear magnetization dependence at 300 K confirms the paramagnetic nature [59]. An apparent hysteresis loop appears at 10 K, with the coercivity ( $H_c$ ) and remnant magnetization ( $M_r$ ), which can be associated with the ferrimagnetic behavior of  $\text{CoCr}_2\text{O}_4$ . The remnant magnetization is found to be 0.3599 emu/g, 0.1578 emu/g and 0.0977 emu/g for  $y = 0, 0.02$  and  $0.03$  concentration, respectively. The coercivity is found to be 3912 Oe, 2581 Oe, and 956 Oe for  $y = 0, 0.02$ , and  $0.03$  concentrations, respectively. The magnetization vs. magnetic field curve shows a hysteresis loop also at 95 K temperature, indicating the ferrimagnetic nature of  $\text{Sc}^{3+}$  doped  $\text{CoCr}_2\text{O}_4$  NPs at these temperatures.

### 3.4. Theoretical analysis

The results of DFT calculations for  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  bulk and surface models, concentrating on structural, electrical, and magnetic characteristics, are provided in this section. Following the experimental investigation, the optimal lattice parameters for pure  $\text{CoCr}_2\text{O}_4$  and Sc-doped models were estimated as  $a = 8.375$  and  $a = 8.423$ , respectively, suggesting a unit cell expansion (Table 1). The M—O bond lengths accompany such volume expansion (Table S2 - Supporting

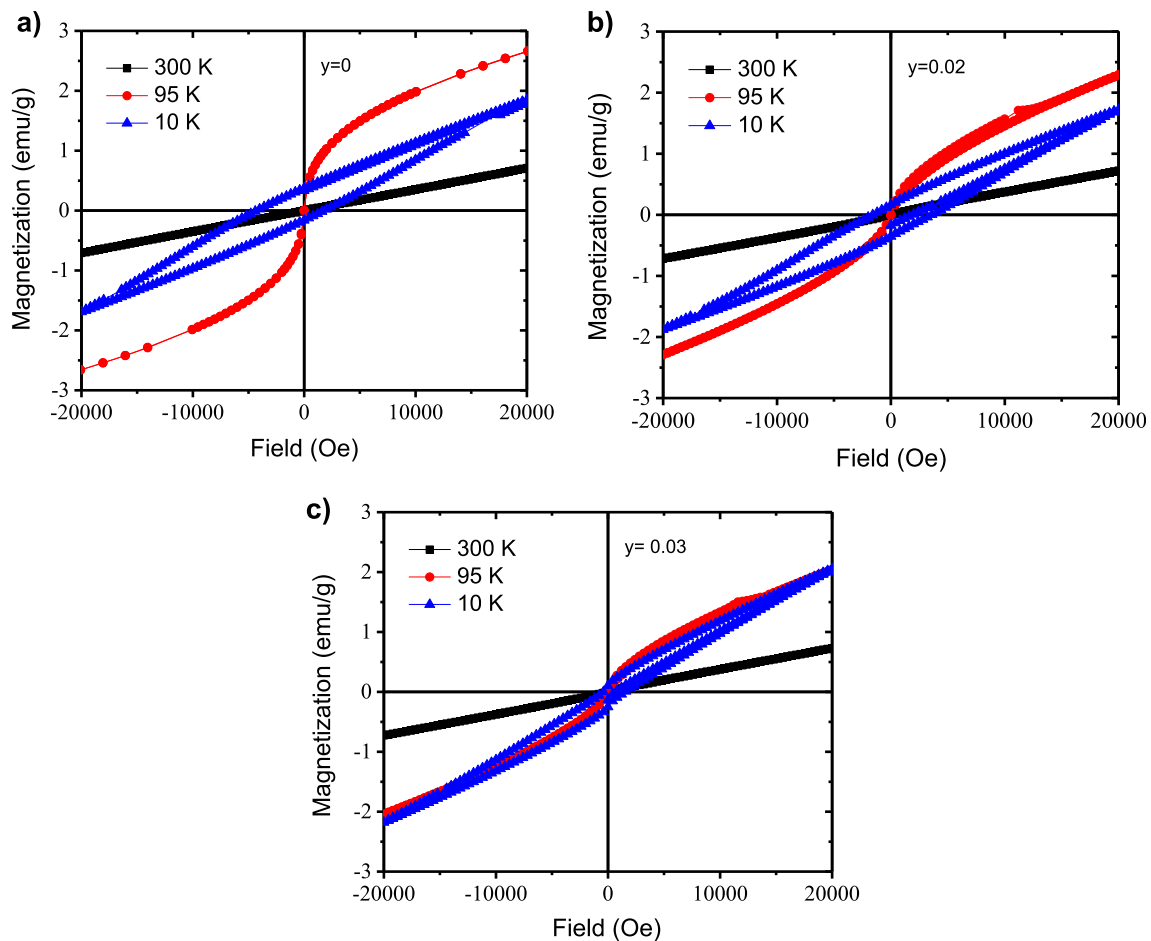


Fig. 5. Field dependent magnetization at 300 K, 95 K and 10 K for  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  a)  $y = 0$ , b)  $y = 0.02$  and c)  $y = 0.03$  NPs.

Table 2

Exchange coupling constants calculated for both pure and Sc-doped  $\text{CoCr}_2\text{O}_4$  models.

|   | $\text{CoCr}_2\text{O}_4$ | $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$ | $\text{Co}_{1-x}\text{Sc}_x\text{Cr}_2\text{O}_4^a$ |
|---|---------------------------|--|---|
| $J_{\text{Co-Co}}$  | -57.51                    | -99.11                                   | -50.53  |
| $J_{\text{Cr-Cr}}$  | -46.41                    | -73.19                                   | -74.05  |
| $J_{\text{Co-Cr}}$  | -32.55                    | -55.98                                   | -50.27  |
| $u = 4J_{\text{BB}}^{\text{SB}}/3J_{\text{AB}}^{\text{SA}}$ | 2.07                      | 1.91                                     | 2.10  |

<sup>a</sup> Ref. [33].

Information), where it was visualized the local structural disorder in the B-site of  $\text{CoCr}_2\text{O}_4$ , resulting in larger Sc-O bonding paths that spread along with the entire crystalline structure, inducing some larger Co-O and Cr-O bond distances closer to the doping site.

The exchange coupling constants were used to examine the bulk magnetic characteristics of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$ , as reported in Table 2.

As a result, we may claim that Sc doping in conjunction with the A- or B-sites of  $\text{CoCr}_2\text{O}_4$  causes structural disorders that control exchange-coupling interactions. The B-site doping is the most advantageous mechanism for inducing a multiple AFM environment for all magnetic interactions. This fact is demonstrated by comparing the computed exchange-coupling constant to the  $T_c$  values provided in the preceding section.

Therefore, we can argue that Sc doping and A- or B-site of  $\text{CoCr}_2\text{O}_4$  induce structural disorders that govern the exchange-coupling interactions. The B-site doping is the most favorable mechanism to induce several AFM environments for all magnetic interactions. This fact can be proved by comparing the calculated exchange-coupling constant with the  $T_c$  values reported in the previous section. Herein, increasing the

AFM extent for all A-A, A-B, and B-B magnetic interaction, the  $T_c$  values decrease with the Sc-content once the ferrimagnetic ordering resulting from dominant  $J_{\text{Co-Co}}$  interactions becomes smaller due to the increased contribution of  $J_{\text{Co-Cr}}$ . In a Ferrimagnetic Neel model, the A and B-site cations are antiparallely ordered; however, increasing the role of  $J_{\text{Co-Cr}}$ , the ferromagnetic ordering becomes more unstable.

The LKDM model [60] can describe a cubic-spinel compound's magnetic ground state and magnetic frustration. The estimated  $u$  values for pure and Sc-doped  $\text{CoCr}_2\text{O}_4$  models suggest that the spiral state exists; nevertheless, it is unstable from the LKDM model's bases.

Let us examine the electronic structure of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  using the FiM-1 Neel model, as shown in Fig. 6. The band-gap region of pure  $\text{CoCr}_2\text{O}_4$  (Fig. 6a) exhibits a band-gap of 4.77 eV (X-X) for the majority spin-channel involving the Cr and Co (3d) orbitals hybridized with O (2p) states. Furthermore, the electron density redistribution for the Sc-doped model (Fig. 6b) reduces the band-gap to 4.63 eV ( $\Gamma$ - $\Gamma$ ).

Compared with our previous study for A-site Sc doping [41], the B-site cation doping contribution for band-gap narrowing is small, associated with the isoelectronic replacement of  $\text{Cr}^{3+}$  by  $\text{Sc}^{3+}$  not requiring

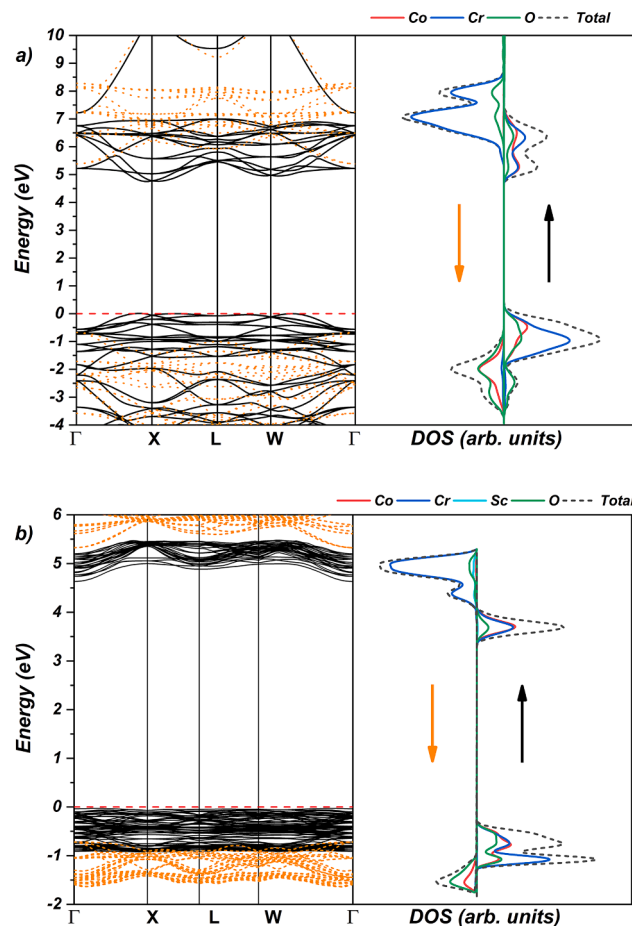


Fig. 6. Theoretical results for Density of States and Band Structure profiles for (a)  $\text{CoCr}_2\text{O}_4$  and (b)  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  models.

the creation of neighboring vacant sites to maintain the supercell neutrality. This fact is an interesting contribution that can guide future studies for doped  $\text{CoCr}_2\text{O}_4$  regarding the electronic properties once the A-site cation doping induces a higher electronic structure disorder with intermediary energy levels from vacant sites than B-site doping.

Despite the essential features reported for bulk models, the precise understanding of surface magnetism is a crucial step in developing multifunctional nanomagnetism. Herein, the (100), (110), (111), and (311) surfaces of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  were investigated using DFT/PBE0 formalism with an atom-centered basis set. The chemical environment of the most stable surface terminations for each investigated plane is depicted in Fig. 7, highlighting the existence of  $[\text{CrO}_n]$  and  $[\text{ScO}_n]$  clusters on the surface.

The (311) surface is the most stable surface for a sizeable thermodynamic region in the phase diagram, exposing  $[\text{CrO}_5]$ ,  $[\text{ScO}_3]$ , and  $[\text{CoO}_2]$  clusters. Moreover, the (110) and (111) become more stable for the Co-poor environment. In this case, the first one exposed  $[\text{ScO}_3]$  and  $[\text{CrO}_3]$  clusters, while the (111) surface plane exhibits similar clusters with the presence of  $[\text{CoO}_2]$ . On the other hand, the (100) surface showed the smallest stable region in phase-diagram showing  $[\text{CrO}_5]$ ,  $[\text{ScO}_5]$ , and  $[\text{CoO}_2]$  exposed clusters. Based on the calculated surface energy values, different morphologies were proposed by  $\text{CoCr}_2\text{O}_4$  NPs. It is worth mentioning that for the Co-poor region, a corner-truncated octahedral shape was found for the Cr-rich region, exposing the significant extent of (111) and (110) surfaces with a minor contribution from (100), changing for a cubic-truncated and corner-truncated icosahedral shape moving to a poor Cr-region with the control of surface exposure for (110) surface. Further, for intermediary and rich Co-composition, a generally rhombic shape containing a significant extent of (311) surface with a minor contribution of other planes was found, following the

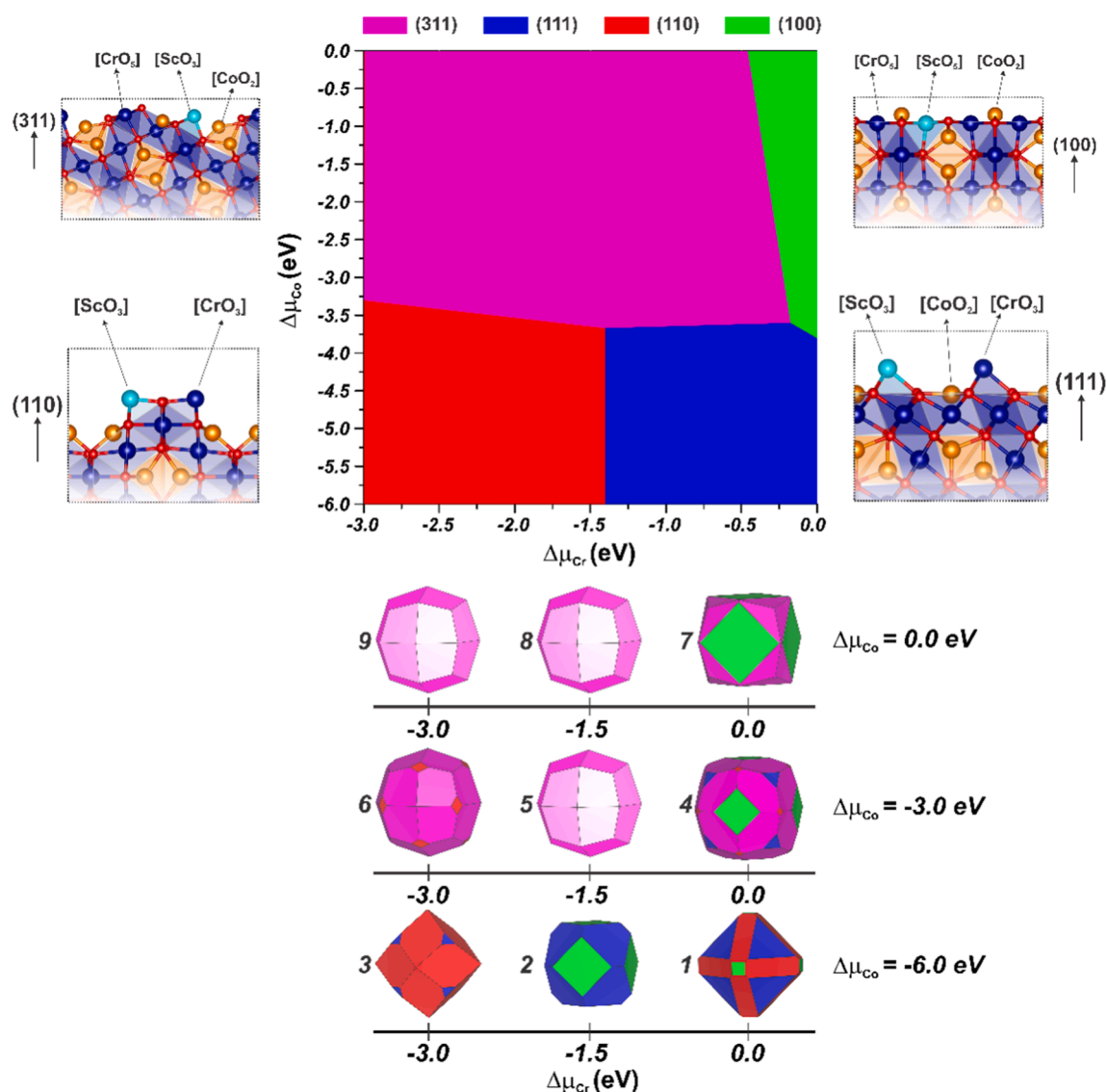
experimental data reported combining TEM and SAED patterns (Fig. 2).

The major aspect of such analysis depends on the surface spin density ( $D_n$ ) for  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  models that enables the calculation of magnetization index (M) for the obtained morphologies, as reported in Table 3. Comparing the spin density before and after Sc-doping, the obtained results indicate that (100) and (111) surfaces showed increased surface magnetism, while (110) and (311) exhibits reduced spin density values. Moreover, for (311) surface, the reduced spin density is associated with the reduced numbers of exchange interactions in the exposed surfaces, once the isoelectronic replacement of  $\text{Cr}^{3+}$  by non-magnetic  $\text{Sc}^{3+}$  induces a stronger magnetic A-B site interaction resulting in an antiparallel arrangement.

Furthermore, the reduced spin density for (311) and (110) surfaces induces a shape-selective control of the nanomagnetism for Sc-doped  $\text{CoCr}_2\text{O}_4$  particles. In particular, the (311)-based shape dominates the phase diagram showing reduced uncompensated spins, contributing to tailor the magnetic properties of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  NPs.

#### 4. Conclusions

The magneto-structural properties of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$  NPs were studied in detail from experimental and theoretical efforts. The spinel cubic structure was confirmed for all samples, exhibiting a unit cell expansion resulting from the local structural disorder associated with the larger ionic radius for  $\text{Sc}^{3+}$ . The morphological analysis combined with Wulff construction confirmed the non-regular shape of the obtained samples, enclosing the (311), (110), and (111) planes. Experimental and theoretical results indicate two magnetic transitions at  $T_C$  and  $T_S$ , where the transition temperature decreases with an increase in  $\text{Sc}^{3+}$  concentration, confirming the magneto-structural behavior associated with the



**Fig. 7.** Surface phase diagram and chemical environment for (100), (110), (111), and (311) surfaces of  $\text{CoCr}_{2-y}\text{Sc}_y\text{O}_4$ . Adapted from Ref. [32] with permission from The Royal Society of Chemistry.

**Table 3**

Spin density ( $D_{\text{H}}$ ) and Magnetization index (M) for the pure and Sc-doped  $\text{CoCr}_2\text{O}_4$  surfaces.

| Surface      | $D_{\text{H}}$ ( $\mu_{\text{B}} \text{nm}^{-2}$ ) |          |
|--------------|--|----------|
|              | Pure   | Sc-doped |
| (100)        | 11.27  | 14.52    |
| (110)        | 16.25  | 14.11    |
| (111)        | 6.55   | 8.19     |
| (311)        | 12.71  | 1.96     |
| Morphologies | M values   |          |
| 1            | 12.05  | 11.69    |
| 2            | 13.38  | 12.63    |
| 3            | 15.92  | 13.90    |
| 4            | 12.25  | 4.49     |
| 5            | 12.75  | 2.13     |
| 6            | 12.87  | 2.51     |
| 7            | 11.92  | 8.82     |
| 8            | 12.71  | 1.96     |
| 9            | 12.71  | 1.96     |

octahedral B-site doping, as confirmed by calculated exchange-coupling constants. The coercivity and remanent magnetization values decrease with an increase in  $\text{Sc}^{3+}$  concentration, following the spin density values calculated for (311) surface that induces an overall control of shape-selective nanomagnetism for  $\text{CoCr}_2\text{O}_4$  NPs.

#### CRediT authorship contribution statement

**V. Jagadeesha Angadi:** Conceptualization, Methodology, Investigation, Writing – review & editing, Project administration. **K. Manjunatha:** Conceptualization, Methodology, Investigation, Data curation, Writing – review & editing. **Marisa C. Oliveira:** Conceptualization, Formal analysis, Investigation, Writing – review & editing, Visualization. **Elson Longo:** Writing – review & editing, Visualization, Funding acquisition. **Sergio R. de Lázaro:** Writing – review & editing, Visualization, Funding acquisition. **Renan A.P. Ribeiro:** Conceptualization, Investigation, Writing – review & editing, Visualization, Supervision, Project administration. **S.V. Bhat:** Writing – review & editing, Visualization, Supervision, Project administration.



## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Appendix A. Supplementary material

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.apsusc.2021.151555>.

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